### **Cryptography: information**

confidentiality, integrity, authenticity, person-identification

## Symmetric cryptography ------ Asymmetric cryptography Diffie-Hellman 1976

Symmetric encryption:	Asymmetric encryption
block ciphers	E-signature - Public Key Infrastructure - PKI
•	E-money
stream ciphers	E-voting
H-functions, Message digest	6
, 6 6	Digital Rights Management - DRM (Marlin)
HMAC H-Message Authentication Code	Etc.
	200

A cryptographic hash function is a special class of hash function that has	
certain properties which make it suitable for use in <u>cryptography</u> . It is a	finite length M - message
mathematical <u>algorithm</u> that <u>maps</u> data of arbitrary finite size to a <u>bit</u>	9
string of a fixed size (a hash function) which is designed to also be a one-	h = H(M)
way function, that is, a function which is infeasible to invert.	<b>~</b>
The only way to recreate the input data from an ideal cryptographic hash	h  = 256 bits
function's output is to attempt a <u>brute-force search</u> of possible inputs to	h = 28 bits
see if they produce a match.	
The input data is often called the <i>message</i> , and the output (the <i>hash</i>	= 7 hex numb.
<i>value</i> or <i>hash</i> ) is often called the <i>message digest</i> or simply the <i>digest</i> .	$OOOO_h = O_h \equiv O_d$
	<b>3</b>
	$0001_{b} = 1_{h} = 1_{d}$
	$0010_{b} = 2_{h} \equiv 2_{d}$
,	$1001_{b} = g_{h} = g_{10}$
	$10.10_{b} = A_{h} = 10_{10}$
	$1110_{b} = E_{h} = 14_{10}$
	h = 1/10
	$1111_{b} = F_{h} = 15_{10}$
	$\bigcirc$

Cryptographic hash functions have many <u>information-security</u> applications, notably in <u>digital</u> <u>signatures</u>, <u>message authentication codes</u> (HMACs), and other forms of <u>authentication</u>. They can also be used as ordinary <u>hash functions</u>, to index data in <u>hash tables</u>, for <u>fingerprinting</u>, to detect duplicate data or uniquely identify files, and as <u>checksums</u> to detect accidental data corruption. Indeed, in information-security contexts, cryptographic hash values are sometimes called (*digital*) *fingerprints*, *message digest* or just *hash values*, even though all these terms stand for more general functions with rather different properties and purposes.

M - message; H(M) = h $M \in \{0, 1\}^{*}$ ;  $h \in \{0, 1\}^{256}$ ;  $H : \{0, 1\}^{*} \rightarrow \{0, 1\}^{256} / SHA256$ Preimage Image 16B - 256 bits - hi many-to-one M20  $H(M_1) = H(M_2) = H(M_3) = ... = h_1$ For given h, it is infeasible to find any Mi satisfying:  $H(M_i) = h_1$ Input Digest cryptographic 40 Hex numbers = 160 bits DFCD 3454 BBEA 788A 751A Fox hash 696C 24D9 7009 CA99 2D17 function SHÀ-1 The red fox cryptographic 0086 46BB FB7D CBE2 823C SHA-1: {0,1}\* ~ {0,1}160 jumps over hash ACC7 6CD1 90B1 EE6E 3ABC the blue dog function Avelange effect The red fox cryptographic 8FD8 7558 7851 4F32 D1C6 jumps ouer hash 76B1 79A9 0DA4 AEFE 4819 the blue dog function 2 100 Birtolay > 2 80 The red fox cryptographic FCD3 7FDB 5AF2 C6FF 915F jumps oevr hash D401 COA9 7D9A 46AF FB45 the blue dog function The red fox cryptographic 8ACA D682 D588 4C75 4BF4 jumps oer hash 1799 7D88 BCF8 92B9 6A6C the blue dog function

A cryptographic hash function (specifically <u>SHA-1</u>) at work. A small change in the input (in the word "over") drastically changes the output (digest). This is the so-called <u>avalanche effect</u>.

#### Properties

- It is quick to compute the hash value for any given finite message.
- A small change to a message should change the hash value so extensively that the new hash value appears uncorrelated with the old hash value.
- Security properties presented below.

Most cryptographic hash functions are designed to take a <u>string</u> of any finite length as input and produce a fixed-length hash value.

A cryptographic hash function must be able to withstand all known <u>types of cryptanalytic attack</u>. In theoretical cryptography, the security level of a cryptographic hash function has been defined using the following properties:

#### • Pre-image resistance

Given a hash value **h** it should be difficult to find any message **M** such that h = H(M). This concept is related to that of <u>one-way function</u>. Functions that lack this property are vulnerable to <u>first preimage attacks</u>.

#### • Second pre-image resistance

Given an input  $M_1$  it should be difficult to find (different) input  $M_2$  such that  $H(M_1) = H(M_2)$ . Functions that lack this property are vulnerable to <u>second-preimage attacks</u>.

#### Collision resistance

It should be difficult to find any two different messages  $M_1$  and  $M_2$  such that  $H(M_1) = M(M_2)$ . Such a pair is called a cryptographic <u>hash collision</u>. This property is sometimes referred to as *strong collision resistance*. It requires a hash value at least twice as long as that required for preimage-resistance; otherwise **collisions** may be found by a <u>birthday attack</u>.<sup>[2]</sup>

These properties form a hierarchy, in that collision resistance implies second pre-image resistance, which in turns implies pre-image resistance, while the converse is not true in general. [3]

The weaker assumption is always preferred in theoretical cryptography, but in practice, a hashfunctions which is only second pre-image resistant is considered insecure and is therefore not recommended for real applications.

Informally, these properties mean that a <u>malicious adversary</u> cannot replace or modify the input data without changing its digest.

Thus, if two strings have the same digest, one can be very confident that they are identical.

M1=?  $M_2=?$ M<sub>1</sub>  $M_2 = ?$ M H() H() H() h  $h = H(M_1) = H(M_2) = h$ H(M) = h $H(M_1)=H(M_2) = h$ **Collision resistance** Preimage resistance Second preimage resistance Loan contract  $M_1$  - is a valid loan contract. h = H(M\_1); |h| = 256 bits  $M_1 = 1000 \in loan.$  $\begin{array}{l} \mathcal{A}: \ P_{r} K_{A} = \chi \longrightarrow \text{Sign}(P_{r} K_{A}, h) = \mathcal{G}_{h} = (\mathcal{F}_{A}, s_{A}) \\ M_{1}, \mathcal{G}_{h}, \ Pu K_{A} \longrightarrow \mathcal{I}_{0}: \text{finds second preimage } M_{2} \\ \text{to create loan contract for 100000} \in \end{array}$ 

such that  $H(M_1) = H(M_2) = h$ Then the valid signature on M1 is valid also on M2.  $f: h = H(M_2) = \frac{M_2, G_h}{Ver(G_h, h, PuK_A)} = True \qquad 100 000 \in (1100 - 100)$ 100 000 & (instead of 1000E) hd28.m - computing 28 bit length h-value in decimal form h28.m - computing 28 bit length h-value in hexadecimal form sha256.m - computing 256 bit length h-value in hexadecimal form >> sha256('RootHash PrevHash 737327631') ans = F4AE534CD226FAF7998C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE >> h28('RootHash PrevHash 737327631') ans = C51E6DE >> hd28('RootHash PrevHash 737327631') ans = 206694110 >> dec2bin(ans) ans = 1100010100011110011011011110 >> dec2hex(206694110) ans = C51E6DE nonce = 737327631 Illustration h28(1, 3) >> sha256('RootHash PrevHash 737327631') ans = F4AE534CD226FAF799\_8C8424B348E020BA80639A687E93A0B8C5130ED\_C51E6DE C51F6DF >> sha256('RootHash PrevHash 73732763<mark>2</mark>') ans = B856211DF2EE15E30AB770C1A43CE014ECFE573182AFD885B28D96854DBC5F21 >> sha256('RootHash PrevHash 737327633') ans = 9C18C764E347A58E57AC3F7A3C2874D5889A0E802699FEA47EEFF8C03BFEDA69 h28('...')→7 hex numb. hd28('--.')→ decimal num.  $O_{h} \equiv 0000_{2}$ ;  $F_{h} \equiv 1111_{2}$ Commitment P = NPAn illustration of the potential use of a cryptographic hash is as follows: Alice poses a tough math problem to Bob and claims she has solved it. P = NP Bob would like to try it himself, but would yet like to be sure that Alice is not bluffing. Elementary: Sherlock Holms and docto Watson Therefore, Alice writes down her solution, computes its hash and tells Bob the hash value (whilst keeping the solution secret). Then, when Bob comes up with the solution himself a few days later, Alice can prove that she had the solution earlier by revealing it and having Bob hash it and check that it matches the hash value given to him before. (This is an

example of a simple <u>commitment scheme</u>; in actual practice, Alice and Bob will often be computer programs, and the secret would be something less easily spoofed than a claimed puzzle solution).

#### Verifying the integrity of files or messages

#### Main article: File verification

An important application of secure hashes is verification of <u>message integrity</u>. Determining whether any changes have been made to a message (or a <u>file</u>), for example, can be accomplished by comparing message digests calculated before, and after, transmission (or any other event).

For this reason, most <u>digital signature</u> algorithms only confirm the authenticity of a hashed digest of the message to be "signed". Verifying the authenticity of a hashed digest of the message is considered proof that the message itself is authentic.

<u>MD5</u>, <u>SHA1</u>, or <u>SHA2</u> hashes are sometimes posted along with files on websites or forums to allow verification of integrity.<sup>[6]</sup> This practice establishes a <u>chain of trust</u> so long as the hashes are posted on a site authenticated by <u>HTTPS</u>.

#### Password verification[<u>edit</u>]

#### Main article: password hashing

A related application is <u>password</u> verification (first invented by <u>Roger Needham</u>). Storing all user passwords as <u>cleartext</u> can result in a massive security breach if the password file is compromised. One way to reduce this danger is to only store the hash digest of each password. To authenticate a user, the password presented by the user is hashed and compared with the stored hash. (Note that this approach prevents the original passwords from being retrieved if forgotten or lost, and they have to be replaced with new ones.) **The password is often concatenated with a random, non-secret <u>salt</u> value** before the hash function is applied. The salt is stored with the password hash. Because users have different salts, it is not feasible to store tables of <u>precomputed</u> hash values for common passwords. <u>Key stretching</u> functions, such as <u>PBKDF2</u>, <u>Bcrypt</u> or <u>Scrypt</u>, typically use repeated invocations of a cryptographic hash to increase the time required to perform <u>brute force attacks</u> on stored password digests. In 2013 a long-term <u>Password Hashing Competition</u> was announced to choose a

new, standard algorithm for password hashing.

#### Proof-of-work

Main article: <u>Proof-of-work system</u>

A proof-of-work system (or protocol, or function) is an *economic* measure to deter <u>denial of service</u> attacks and other service abuses such as spam on a network by requiring some work from the service requester, usually meaning processing time by a computer. A key feature of these schemes is their asymmetry: the work must be moderately hard (but feasible) on the requester side but easy to check for the service provider. One popular system — used in <u>Bitcoin mining</u> and <u>Hashcash</u> — **uses partial hash inversions to prove that work was done,** as a good-will token to send an e-mail. The sender is required to find a message whose hash value begins with a number of

 $\begin{array}{c} f \neq f' \\ H(f) \neq H(f') \\ h & h' \\ Sign(PrK, h) \neq Sign(PrK, h') \end{array}$ 

# $2^{20} = 1M$

#### File or data identifier

A message digest can also serve as a means of reliably identifying a file; several <u>source code management</u> systems, including <u>Git</u>, <u>Mercurial</u> and <u>Monotone</u>, use the <u>sha1sum</u> of various types of content (file content, directory trees, ancestry information, etc.) to uniquely identify them. Hashes are used to identify files on <u>peer-to-peer filesharing</u> networks.

#### Pseudorandom generation and key derivation

Hash functions can also be used in the generation of <u>pseudorandom</u> bits, or to <u>derive new keys or passwords</u> from a single secure key or password.

As of 2009, the two most commonly used cryptographic hash functions were <u>MD5</u> and <u>SHA-1</u>. However, a successful attack on MD5 broke <u>Transport</u> <u>Layer Security</u> in 2008.

In February 2005, an attack on SHA-1 was reported that would find collision in about 2<sup>69</sup> hashing operations, rather than the 2<sup>80</sup> expected for a 160-bit hash function. In August 2005, another attack on SHA-1 was reported that would find collisions in 2<sup>63</sup> operations. Though theoretical weaknesses of SHA-1 exist, <sup>[14][15]</sup> no collision (or near-collision) has yet been found. Nonetheless, it is often suggested that it may be practical to break within years, and that new applications can avoid these problems by using later members of the SHA family, such as <u>SHA-2</u>.

According to birthday paradox it is not required total scan all  $2^{160}$  variants of message M. It is enough to scan  $\sqrt{2^{160}} = 2^{80}$  variants.

No needed

No needed

SHA-2 (Secure Hash Algorithm 2) is a set of <u>cryptographic hash</u> functions designed by the United States <u>National Security Agency</u> (NSA).<sup>[3]</sup> From <https://en.wikipedia.org/wiki/SHA-2>

SHA-2 includes significant changes from its predecessor, <u>SHA-1</u>. The SHA-2 family consists of six hash functions with <u>digests</u> (hash values) *h 28* that are 224, 256, 384 or 512 bits: **SHA-224, SHA-256, SHA-384, SHA-512, SHA-512/224, SHA-512/256**. However, to ensure the long-term robustness of applications that use hash

functions, there was a <u>competition</u> to design a replacement for SHA-2. On October 2, 2012, Keccak was selected as the winner of the <u>NIST</u> hash function competition.

A version of this algorithm became a <u>FIPS</u> standard on August 5, 2015 under the name SHA-3.

#### **HMAC - H Message Authentication Code**

Use in building other cryptographic primitives: symmetric e-signature realization  $\searrow$ 

Hash functions can be used to build other cryptographic primitives.

For these other primitives to be cryptographically secure, care must be taken to build them correctly.

Message authentication codes (MACs) (also called keyed hash functions) are often built from hash functions. <u>HMAC</u> is such a MAC.

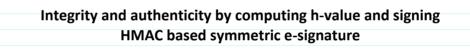
Authentication Integrity

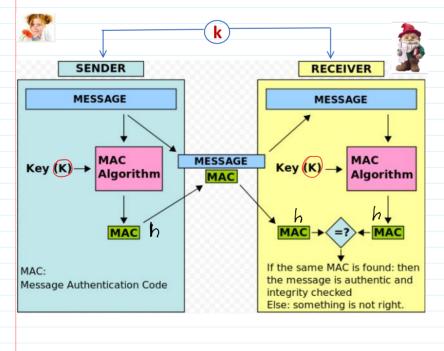
**Keyed-hash message authentication code (HMAC)** is a specific type of <u>message authentication code</u> (MAC) involving a <u>cryptographic hash function</u> (hence the 'H') in combination with a secret <u>cryptographic key</u>. As with any MAC, it may be used to *simultaneously* verify both the <u>data integrity</u> and the <u>authentication</u> of a <u>message</u>.

Any cryptographic hash function, may be used in the calculation of an HMAC.

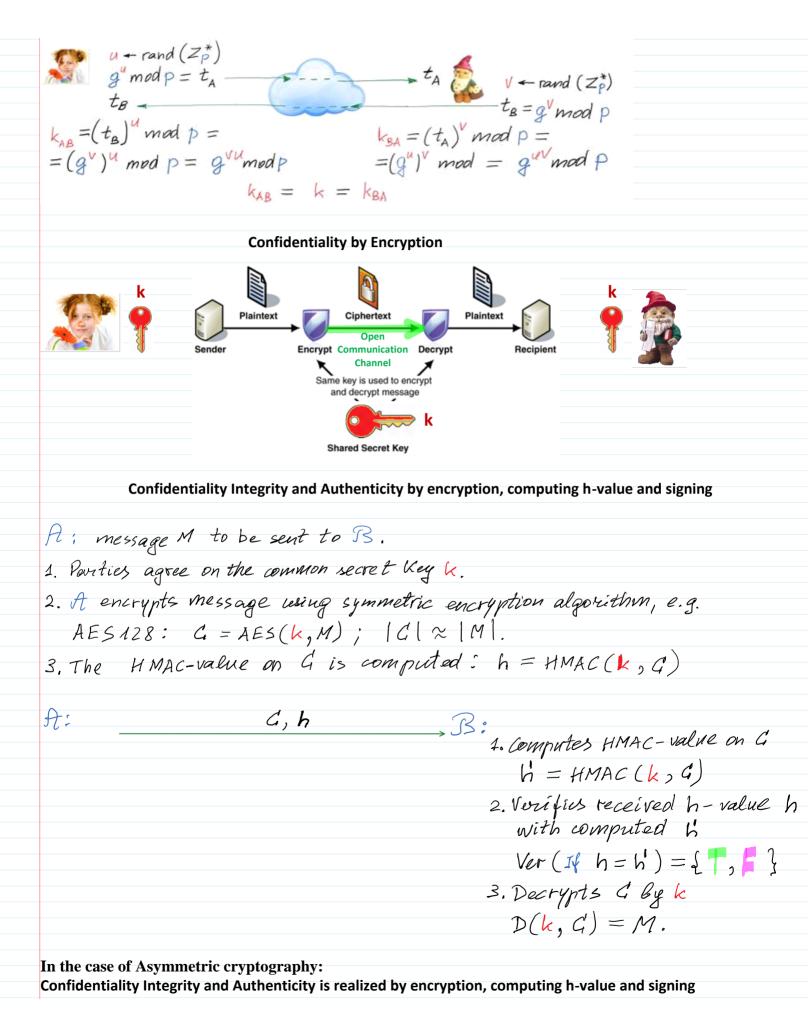
The cryptographic strength of the HMAC depends upon the <u>cryptographic strength</u> of the underlying hash function, the size of its hash output, and on the size and quality of the key.

Public Parameters PP=(p,g)





Public Parameters PP = (p, g)



A: message M to be sent to B. 1. Pourties agree on the common secret Key K. 2. A encrypts message using symmetric encryption algorithm, e.g. AES128: C = AES(k, M);  $|C| \approx |M|$ . 3. The h-value of G is computed: h = sha256(G)4. The signature is placed on h: Sign(PrKA, h) = o = (r, s)  $\mathcal{B}: \mathcal{P}\mathcal{K}_{\mathbf{B}} = \mathcal{Y}; \mathcal{P}\mathcal{U}\mathcal{K}_{\mathbf{B}} = b.$  $f: P_{r}K_{A} = x; P_{u}K_{A} = a.$ 4. Computes b - value of Gb = sha256(G)2. Vorifics signature on h  $Ver(PuK_A, \delta, h) = [7, [5]]$ 3. Decrypts G by k D(k, G') = M.N I Telecommunik KA2 KA1  $K_{B2}$  $= (K_A)^g mod_p = K_{BA}$  $K_{AB} = (K_B)^{\times} \mod p =$ K  $(\mathcal{K}_{1})$ K2 M - messag  $Enc(K_1, m) = (C_1)$  $Dec(K_1, C_1) = m$ Data center  $ENC(K_2, M) = (C_2) Dec(k_2, c_2) = m$ 

 $Dec(K_2, C_2) = m$ 

 $\geq$ 

CBC-MAC

Backdoors +

>> sha256('RootHash PrevHash 737327631') ans = F4AE534CD226FAF7998C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE >> h28('RootHash PrevHash 737327631') ans = C51E6DE >> hd28('RootHash PrevHash 737327631') ans = 206694110 >> dec2bin(ans) ans = 1100010100011110011011011110 >> dec2hex(206694110) ans = C51E6DE

#### Hash functions based on block ciphers

There are several methods to use a block cipher to build a cryptographic hash function, specifically a one-way compression function. The methods resemble the <u>block cipher modes of operation</u> usually used for encryption. Many well-known hash functions, including MD4, MD5, SHA-1 and SHA-2 are built

from block-cipher-like components

HMAC can be constructed form the block cipher using cipher block chaining  $AES_{L-}CBC$ (CBC) mode of operation.

M - to be signed.  $G = AES_CBC(k, M)$ 256

Cipher block chaining message authentication code (CBC-MAC) is a technique for constructing a message authentication code from a block cipher. The message is encrypted with some block cipher algorithm in CBC

mode to create a chain of blocks such that each block depends on the proper encryption of the previous block.

This interdependence ensures that a change to any of the plaintext bits will cause the final encrypted block to change in a way that cannot be predicted or counteracted without knowing the key to the block cipher.

From <https://en.wikipedia.org/wiki/CBC-MAC>

 $||_{k}| = 256 b \implies B_{i} = C_{i} = 256$ 

6: CI C2 --- CN

hMAC=  $G_1 \oplus G_2 \oplus \ldots \oplus G_N = h$ bitwice XORing 1h) = 256 b.

Plaintext **B**N

Initialization Vector (IV)

Plaintext B1

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bitwice XORing Plaintext B1 Plaintext B2 Plaintext B<sub>N</sub> (h) = 256 b. Initialization Vector (IV) ¢ ¢ Ð block cipher block cipher block cipher Key Key Key encryption encryption encryption Ciphertext C<sub>1</sub> Ciphertext C<sub>N</sub> Ciphertext C<sub>2</sub> Cipher Block Chaining (CBC) mode encryption Chosep Plaintext Attack A:  $\mathcal{B}: \mathcal{H}_{cBc}(k, c) = h'$  $E_{cBc}(k, m) = c \qquad encrypt c, h$   $H_{cBc}(k, c) = h \qquad hash$ ? h Z h' if ok 2)  $\mathbb{D}(k,c) = m$